

ISTEP+: Algebra I

**End-of-Course Assessment** 

Released Items and Scoring Notes

#### Introduction

Indiana students enrolled in Algebra I participated in the *ISTEP+: Algebra I Graduation Examination* End-of-Course Assessment (ECA) during the 2012-2013 test administration windows. The Algebra I ECA consists of four item types which contribute to a student's scale score: multiple-choice, constructed-response, gridded-response and graphing items. It is important to keep in mind that a significant portion of a student's score is calculated from the multiple-choice items on the assessment, which are not addressed within this document.

This document consists of constructed-response and graphing items from the Spring 2013 administration and includes:

- Sample released open-ended questions
- Rubrics used by trained evaluators to score student responses
- Sample papers used by trained evaluators to distinguish between rubric score point values
- Annotations describing the rationale for scoring student responses

The purpose of this guide is to provide additional Algebra I ECA sample items and to model the types of items that are scored using rubrics.

#### **Reporting Category 1: Solving Linear Equations and Inequalities**

#### **Question 1**

Last year, the area of Jamie's garden was 32 square feet. This year, she added a new rectangular-shaped section to her garden. The length of the new section of the garden is 12 feet. The TOTAL area of her garden now, last year's garden plus the new section, is 116 square feet.

Write an equation that can be used to determine the width (w), in feet, of the new section of the garden.

Answer_	 

What is the width, in feet, of the new section of the garden?

Answer_	 	 	

### **Exemplary Response:**

• 32 + 12w = 116

Or other equivalent equation

And

• 7 (feet)

#### **Rubric:**

**2 points:** Exemplary response. Correct equation in Part A and correct solution in Part B.

**1 point:** Correct equation in Part A or correct solution in Part B. Or, correct solution in Part B

based on an incorrect linear equation in Part A, given that one of the two necessary

steps to solve the problem are done correctly.

### Question 1, Sample A – 2 points

**Part A:** 84 = 12x **Part B:** 7 feet

Notes: This response is equivalent to the exemplary response.

### **Question 1, Sample B – 1 point**

**Part A:** (116 - 32)/12 = W

Part B: 6.5 feet

Notes: The response for Part A is correct; however, the response for Part B is

incorrect.

### **Question 1, Sample C – 1 point**

**Part A:** (32)(12x) = 116

**Part B:** w = 7ft

Notes: The response for Part B is correct; however, the response for Part A is

incorrect.

### Question 1, Sample D-0 points

**Part A:**  $32 \times 12 = w$ 

**Part B:** 464ft

Notes: Part A and B are both incorrect.

### Reporting Category 3: Systems of Linear Equations and Inequalities

### **Question 2**

In the fall, a community service club sold 10 shirts and 20 hats for a total of \$490. In the spring, the club sold 20 shirts and 30 hats for a total of \$860.

Each shirt sold for the same price. Each hat sold for the same price.

Write a system of equations that can be used to find the cost, in dollars, of one shirt (s) and one hat (h).

Answer	 	

What is the total cost, in dollars, of one shirt and one hat?

Answer_	 	 	 

### **Exemplary Response:**

$$10s + 20h = 490$$

$$20s + 30h = 860$$

Or other equivalent system of equations

#### And

• \$37.00

Note: Student receives full credit if response given indicates separately that one shirt costs \$25.00 and one hat costs \$12.00.

#### **Rubric:**

**2 points:** Exemplary response. Correct system given in Part A and correct value given in Part B.

1 point: One key element. Correct system of equations only. Or, correct value in Part B only. Or, a correct answer in Part B based on an incorrect system of equations given in Part A.

### Question 2, Sample A - 2 points

**Part A:** 10s + 20h = 490; 20s + 30h = 860

**Part B:** \$37

*Notes: This response is equivalent to the exemplary response.* 

### **Question 2, Sample B – 1 point**

**Part A:** 10s + 20h = 490; 20s + 30h = 860

**Part B:** h = 12 and s = 37

Notes: The response for Part A is correct; however, the solution in Part B is

incorrect.

### **Question 2, Sample C – 1 point**

**Part A:** 10s + 20h = 490

**Part B:** s = 25 and h = 12

Notes: The response for Part B is correct; however, Part A only gives one of the

two correct equations.

### **Question 2, Sample D – 0 points**

**Part A:** 10x + 30x = 860

**Part B:** \$17.50

Notes: Part A and B are both incorrect.

### Reporting Category 2: Graphing and Interpreting Linear and Non-Linear Relations

### **Question 3**

A line passes through the points (4, -7) and (-5, 8).

What is the slope of this line?

Answer		

Write an equation that represents this line.

Answer	 	 	

## **Exemplary Response:**

• 
$$m = -\frac{5}{3}$$

And

$$\bullet \quad y = -\frac{5}{3}x - \frac{1}{3}$$

Or other equivalent equation

#### **Rubric:**

**2 points:** Exemplary response. Correct slope and correct equation.

1 point: Correct slope or correct equation. Or, correct equation based on an incorrect slope.

### Question 3, Sample A - 2 points

**Part A:** 
$$m = -\frac{5}{3}$$

**Part B:** 
$$y = -\frac{5}{3}x - \frac{1}{3}$$

Notes: This response is equivalent to the exemplary response.

### Question 3, Sample B – 1 point

**Part A:** 
$$-\frac{5}{3}$$

**Part B:** 
$$y = -\frac{5}{3}x + \frac{41}{3}$$

Notes: The response for Part A is correct; however, the response for Part B is incorrect.

### **Question 3, Sample C – 1 point**

**Part B:** 
$$y = 0.5x - 9$$

Notes: The response for Part A is incorrect; however, the response for Part B gives a correct equation based on the incorrect slope in Part A.

### **Question 3, Sample D – 0 points**

**Part A:** 
$$m = 9$$

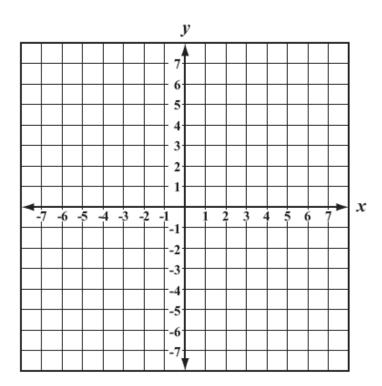
**Part B:** 
$$y = 9x - 15$$

Notes: Part A and B are both incorrect.

# **Reporting Category 2: Graphing and Interpreting Linear and Non-Linear Relations**

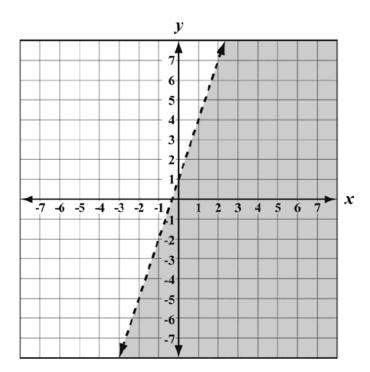
## **Question 4**

**Graph:** y < 3x + 1



### **Exemplary Response:**

• The graph of y < 3x + 1.



#### **Rubric:**

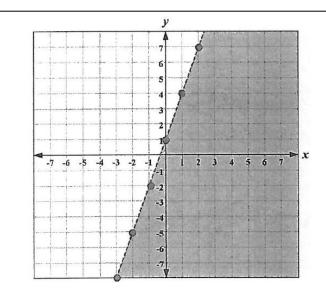
**2 points:** Exemplary response.

**1 point:** The graph of y = 3x + 1 using a solid or dashed line with incorrect or no shading. Or,

an incorrect dashed line shaded correctly. Note: if more than 1 line is graphed or

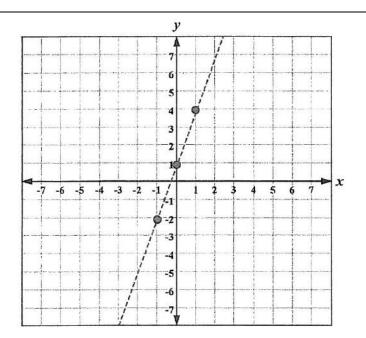
additional incorrect points are potted, no points will be awarded.

# **Question 4, Sample A – 2 points**



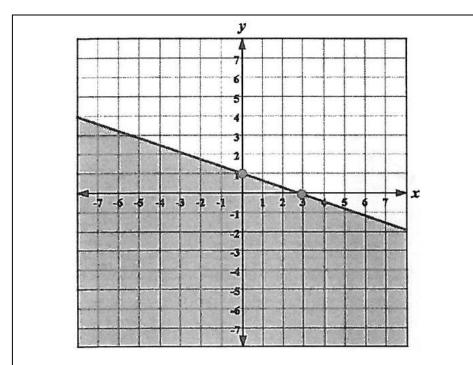
Notes: This response is equivalent to the exemplary response.

## **Question 4, Sample B – 1 point**



Notes: This response shows the graph of y = 3x + 1 using a dashed line; however, the proper region is not shaded.

## Question 4, Sample C-0 points



Notes: This response is incorrect and receives a score of zero points.

### **Reporting Category 1: Solving Linear Equations and Inequalities**

### **Question 5**

Ben tried to solve the inequality 6x - 1 > 4 + 3(x - 2). He made an error. His work is shown below.

$$6x - 1 > 4 + 3(x - 2)$$

$$6x - 1 > 4 + 3x - 6$$

$$6x - 1 > 3x - 2$$

$$3x - 1 > -2$$

$$3x > -1$$

$$x < -\frac{1}{3}$$

What error did Ben make?

Solve: 6x - 1 > 4 + 3(x - 2)

Answer\_\_\_\_

### **Exemplary Response:**

• He flipped the inequality symbol. Or, he should not have flipped the inequality symbol.

Or other acceptable description of the error. Note: response may reference what was done incorrectly or what should have been done correctly.

#### And

$$\bullet \quad x > -\frac{1}{3}$$

#### **Rubric:**

2 points: Exemplary response. Correct description in Part A and correct solution in Part B.

**1 point:** Correct description in Part A or correct solution in Part B.

### Question 5, Sample A - 2 points

**Part A:** His inequality sign is going the wrong way in the last line of his work.

**Part B:** x > -1/3

Notes: This response is equivalent to the exemplary response.

### **Question 5, Sample B – 1 point**

**Part A:** He changed the inequality from > to this < when he should have kept it the same.

**Part B:** x = 1

Notes: Part A provides a valid response; however, Part B is incorrect.

### Question 5, Sample C - 0 points

**Part A:** he needs to do 4 + - 6

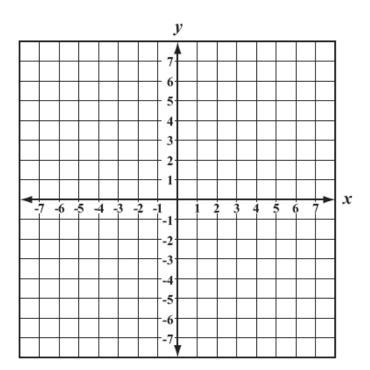
**Part B:** x > -1.3

*Notes: Part A and B are both incorrect.* 

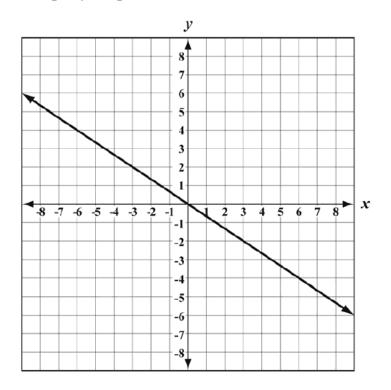
# **Reporting Category 2: Graphing and Interpreting Linear and Non-Linear Relations**

# **Question 6**

**Graph:** 
$$y = -\frac{2}{3}x$$



## **Exemplary Response:**



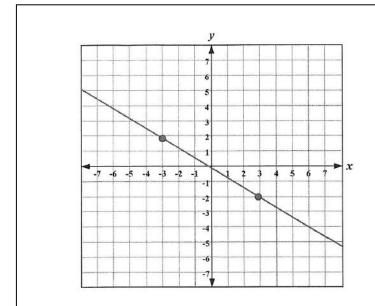
### **Rubric:**

**1 point:** Exemplary response.

**0 points:** Other

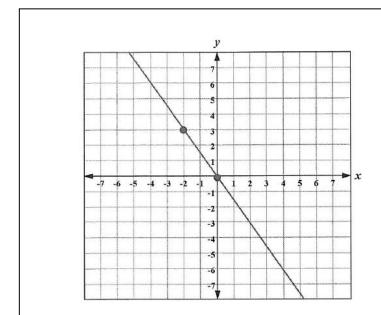
Note: If more than one line is graphed, or additional incorrect points are plotted, no points will be awarded.

## **Question 6, Sample A – 1 point**



Notes: This response is equivalent to the exemplary response.

### **Question 6, Sample B – 0 points**



Notes: This response is incorrect.

### **Reporting Category 5: Solving and Graphing Quadratic Equations**

### **Question 7**

Solve for *x*:  $3x^2 - 8x + 4 = 0$ 

Answer\_\_\_\_\_

### **Exemplary Response:**

 $\bullet \quad x = \frac{2}{3} \text{ and } x = 2$ 

### **Rubric:**

**2 points:** Exemplary response. Two correct solutions.

**1 point:** One correct solution. Or, solutions of  $x = -\frac{2}{3}$  and -2. Or, an answer left

unsimplified, such as,  $x = \frac{8 \pm \sqrt{16}}{6}$ .

## Question 7, Sample A - 2 points

**Answer:** x = 2 and x = 2/3

Notes: This response is equivalent to the exemplary response.

### **Question 7, Sample B – 1 point**

**Answer:** 16, 2

Notes: This response gives one correct solution.

## Question 7, Sample C - 0 points

**Answer:** 2x

Notes: This response is incorrect.

### **Reporting Category 3: Systems of Linear Equations and Inequalities**

### **Question 8**

Solve the system of equations below.

$$y = -4x + 14.5$$

$$2x + 2y = 11$$

Answer_	 	 	

#### **Exemplary Response:**

• (3, 2.5)

#### **Rubric:**

**2 points:** Exemplary response. Correct values for both x and y.

**1 point:** One correct value. Or, correct values switched. Or a correct x-value based on an

incorrect y-value. Or, a correct y-value based on an incorrect x-value.

### Question 8, Sample A - 2 points

**Answer:** x = 3, y = 5/2

Notes: This response is equivalent to the exemplary response.

### **Question 8, Sample B – 1 point**

**Answer:** x = 4, y = 2.5

Notes: This response shows the correct y-value of the system of equations; however, the x-value is incorrect.

## **Question 8, Sample C – 1 point**

**Answer:** x = -3, y = 8.5

Notes: This response gives a correct y-value based on an incorrect x-value using the equation 2x + 2y = 11.

### Question 8, Sample D - 0 points

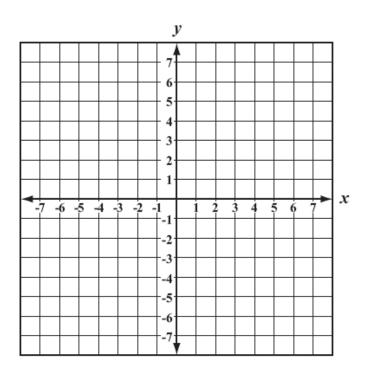
**Answer:** (-2,2)

Notes: This response is incorrect.

# **Reporting Category 2: Graphing and Interpreting Linear and Non-Linear Relations**

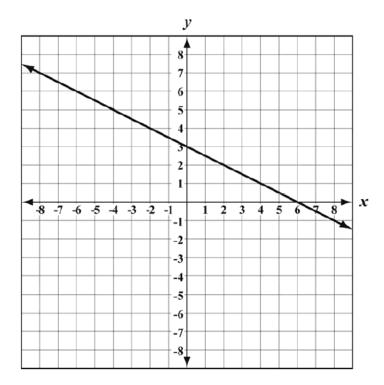
# **Question 9**

**Graph:** 4y = -2x + 12



### **Exemplary Response:**

• The graph of 4y = -2x + 12.



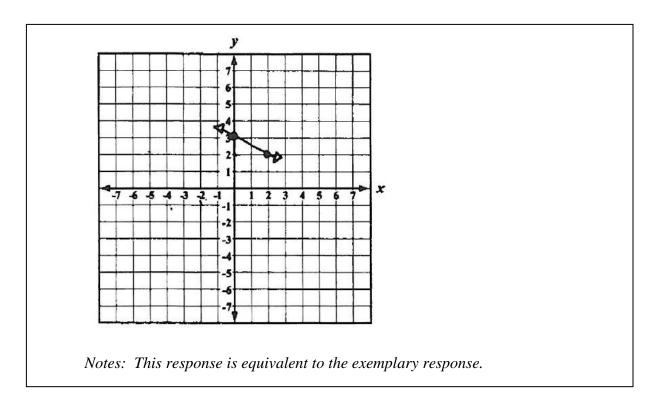
### **Rubric:**

**1 point:** Exemplary response.

**0 points:** Other

Note: If more than one line is graphed, or additional incorrect points are plotted, no points will be awarded.

## **Question 9, Sample A – 1 point**



### **Question 9, Sample B – 0 points**

